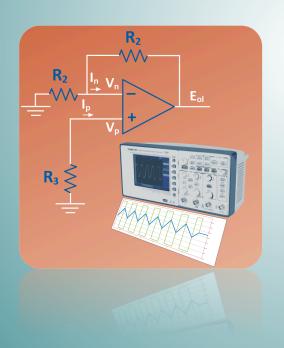




#### Electrónica Básica

Tema B.4. El Amplificador Diferencial



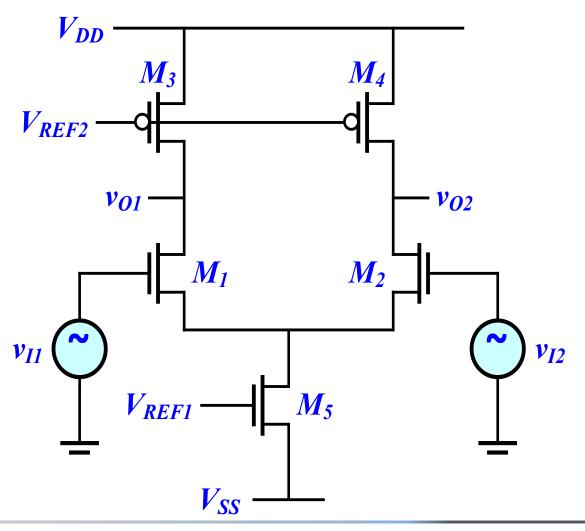
#### Gustavo A. Ruiz Robredo Juan A. Michell Martín

DPTO. DE ELECTRÓNICA Y COMPUTADORES

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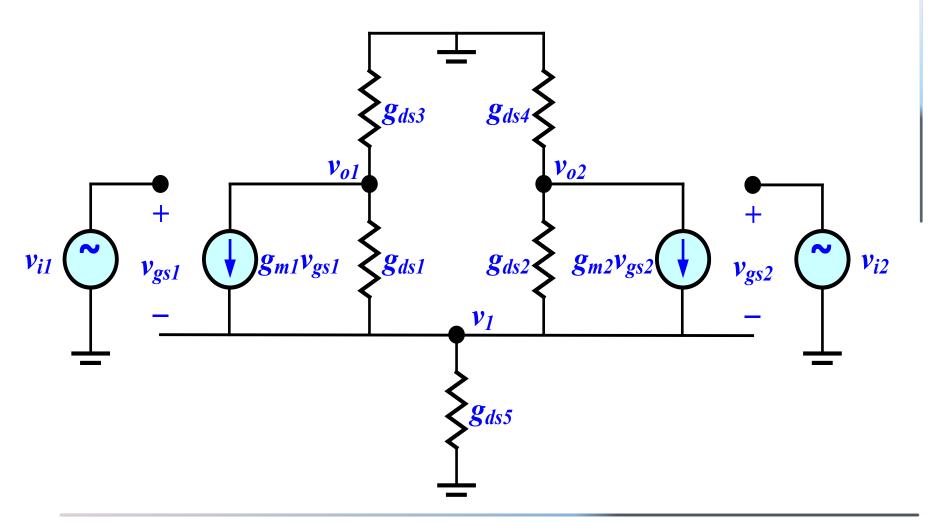


• Esquema de circuito:

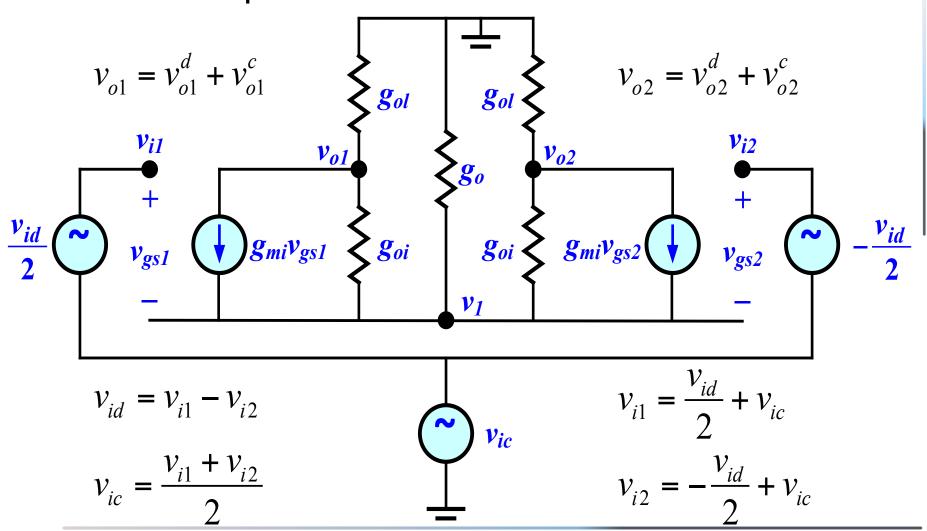




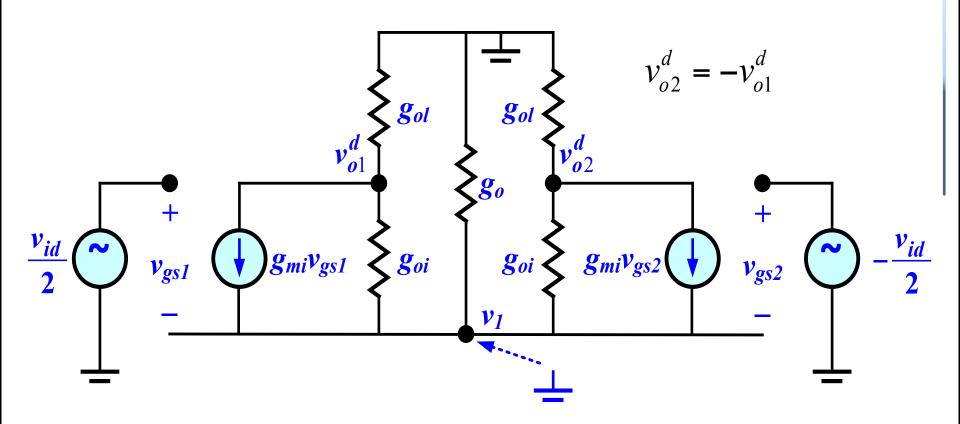
Circuito equivalente de pequeña señal:



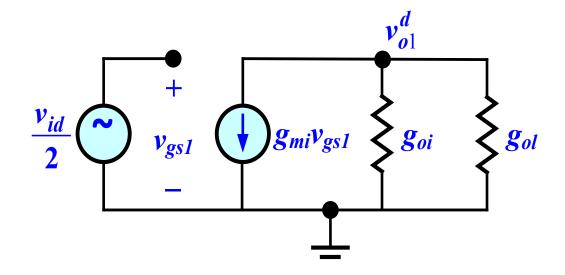
· Circuito equivalente con transistores simétricos:



Análisis en modo diferencia (DM):

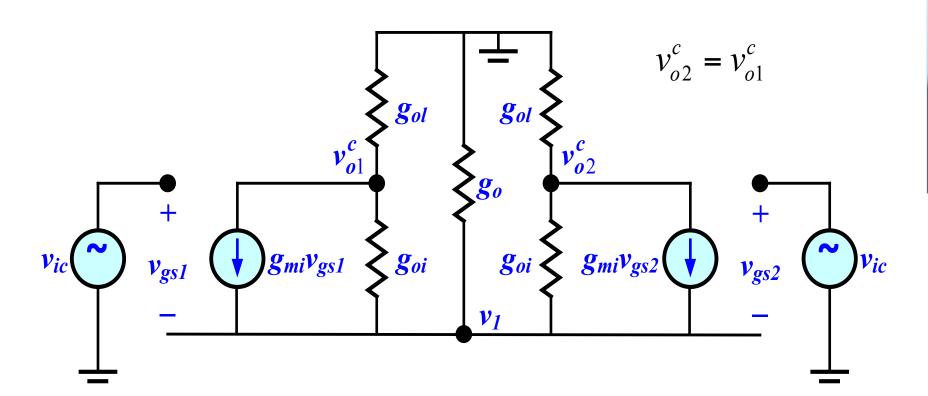


Circuito equivalente de pequeña señal en DM:

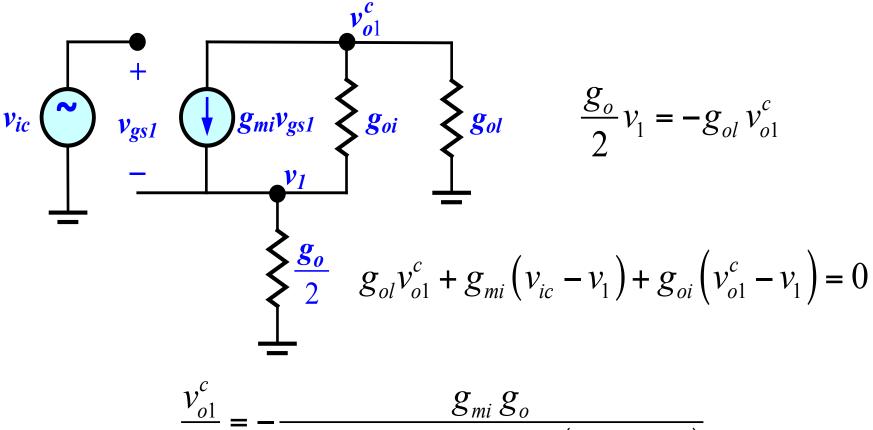


$$v_{o1}^{d} = -\frac{g_{mi}}{(g_{ol} + g_{oi})} \frac{v_{id}}{2}$$

Análisis en modo común (CM):

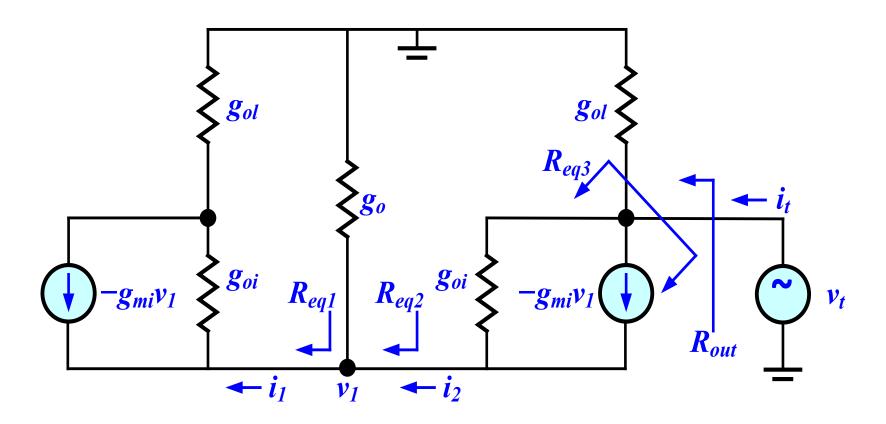


• Circuito equivalente de pequeña señal en CM:

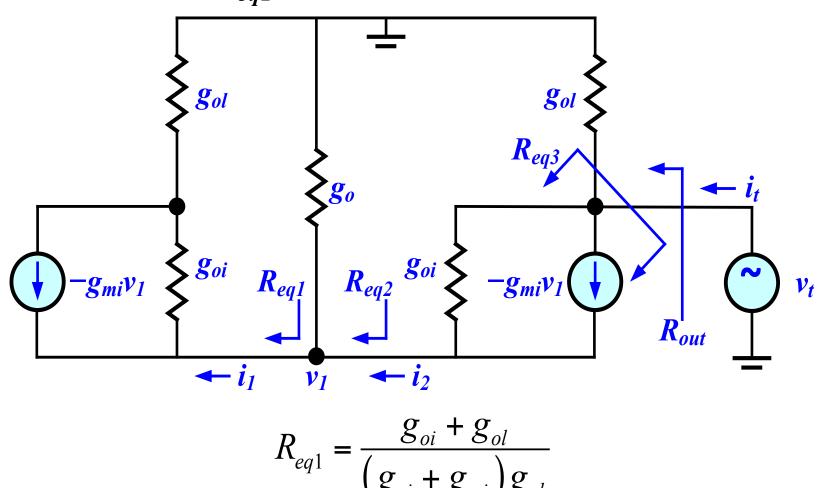


$$\frac{v_{o1}^{c}}{v_{ic}} = -\frac{g_{mi} g_{o}}{g_{oi} g_{o} + g_{ol} g_{o} + 2g_{ol} (g_{mi} + g_{oi})}$$

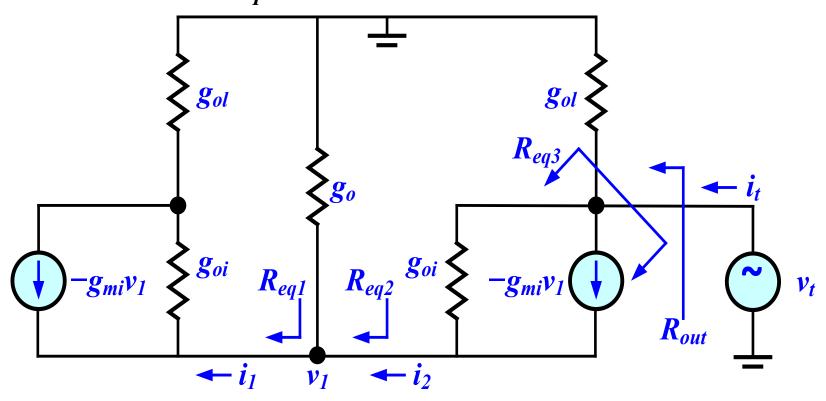
• Resistencia de salida  $R_{out}$ :



• Cálculo de  $R_{eq1}$ :

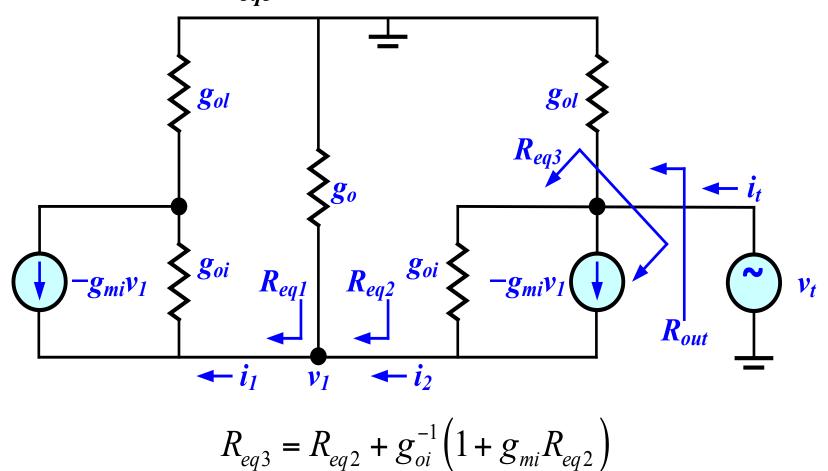


• Cálculo de  $R_{eq2}$ :

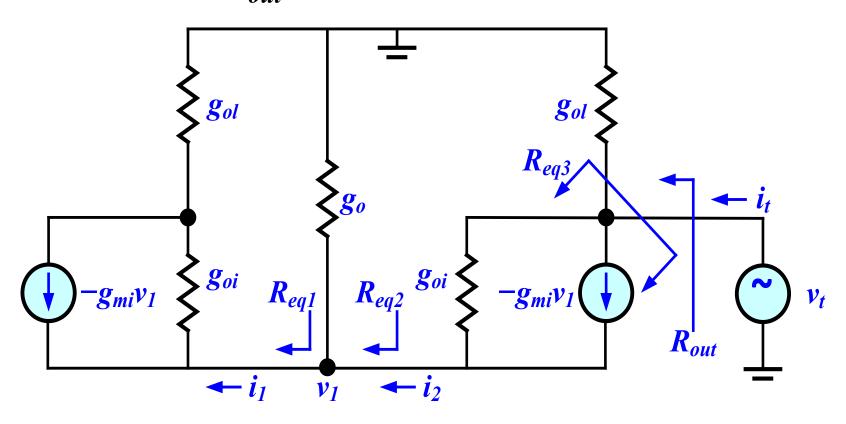


$$R_{eq2} = g_o^{-1} || R_{eq1}$$

• Cálculo de  $R_{eq3}$ :



#### • Cálculo de $R_{out}$ :



$$R_{out} = g_{ol}^{-1} \parallel R_{eq3}$$

Tensiones de salida:

$$v_{o1} = v_{o1}^{d} + v_{o1}^{c}$$

$$v_{o1} = -\frac{g_{mi}}{(g_{ol} + g_{oi})} \frac{v_{id}}{2} - \frac{g_{mi} g_{o}}{g_{oi} g_{o} + g_{ol} g_{o} + 2g_{ol} (g_{mi} + g_{oi})} v_{ic}$$

$$v_{o2} = v_{o2}^{d} + v_{o2}^{c} = -v_{o1}^{d} + v_{o1}^{c}$$

$$v_{o2} = \frac{g_{mi}}{(g_{ol} + g_{oi})} \frac{v_{id}}{2} - \frac{g_{mi} g_{o}}{g_{oi} g_{o} + g_{ol} g_{o} + 2g_{ol} (g_{mi} + g_{oi})} v_{ic}$$



• Ganancias DM  $(A_{dm})$  y CM  $(A_{cm})$ :

$$v_{od} = v_{o1} - v_{o2} = -\frac{g_{mi}}{(g_{ol} + g_{oi})} v_{id}$$

$$A_{dm} = \frac{v_{od}}{v_{id}} = -\frac{g_{mi}}{(g_{ol} + g_{oi})}$$

$$v_{oc} = \frac{v_{o1} + v_{o2}}{2} = -\frac{g_{mi} g_o}{g_{oi} g_o + g_{ol} g_o + 2g_{ol} (g_{mi} + g_{oi})} v_{ic}$$

$$A_{cm} = \frac{v_{oc}}{v_{ic}} = -\frac{g_{mi}}{g_{oi} + g_{ol} + \frac{2g_{ol}(g_{mi} + g_{oi})}{g_{o}}}$$

Razón de rechazo del modo común (CMMR):

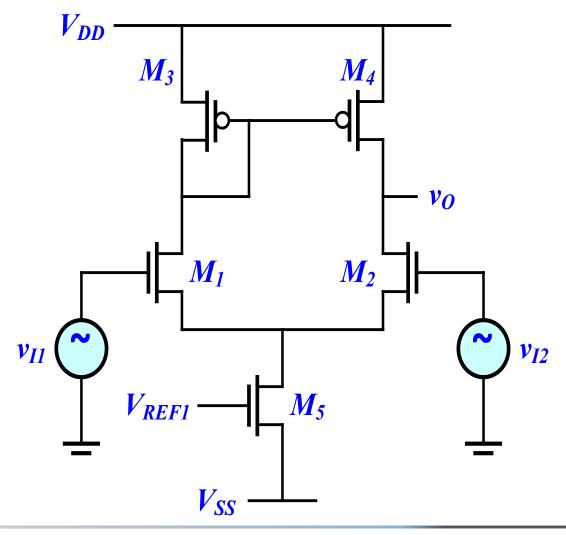
$$CMRR = \left| \frac{A_{dm}}{A_{cm}} \right| = 1 + \frac{2g_{ol}(g_{mi} + g_{oi})}{g_{o}(g_{ol} + g_{oi})}$$

Tensiones de salida vs. tensiones de entrada:

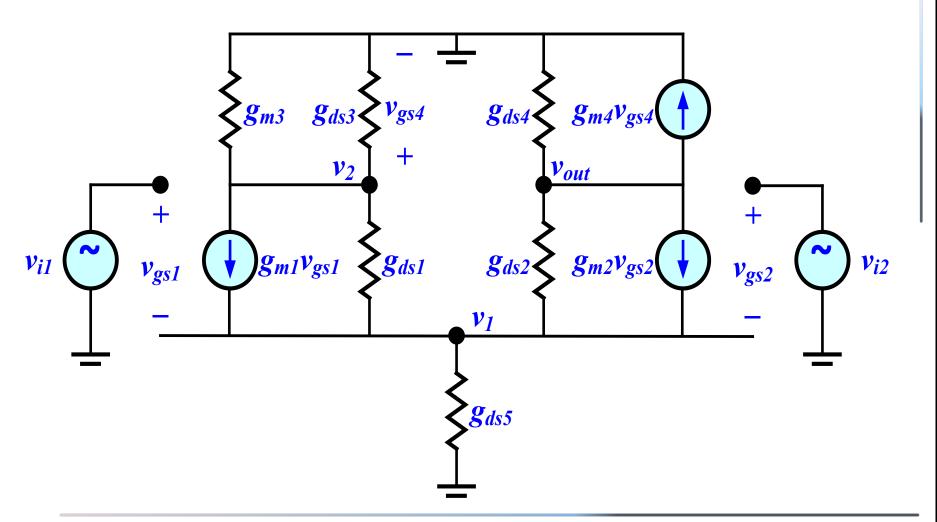
$$v_{o1} = \frac{A_{dm}}{2} (v_{i1} - v_{i2}) + \frac{A_{cm}}{2} (v_{i1} + v_{i2})$$

$$v_{o2} = -\frac{A_{dm}}{2} (v_{i1} - v_{i2}) + \frac{A_{cm}}{2} (v_{i1} + v_{i2})$$

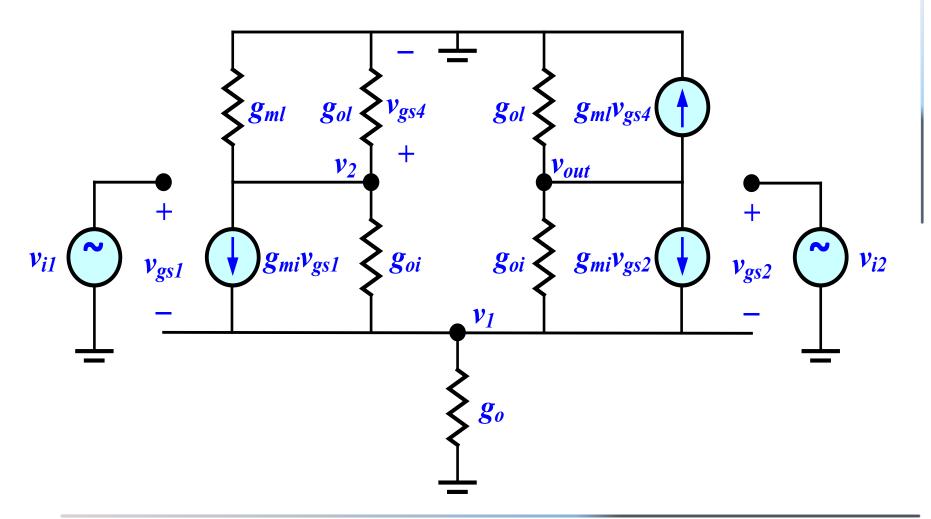
• Esquema de circuito:



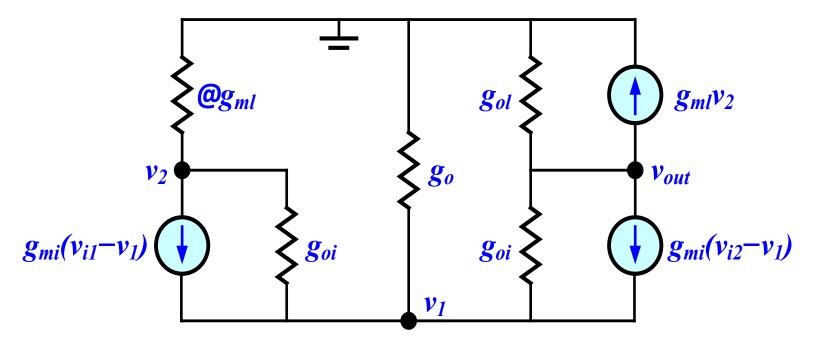
Circuito equivalente de pequeña señal:



Circuito equivalente con transistores simétricos:



Análisis del circuito con transistores simétricos:



$$\begin{split} g_{ml}v_2 + g_{mi}\left(v_{i1} - v_1\right) + g_{oi}\left(v_2 - v_1\right) &= 0 \\ -g_ov_1 + g_{oi}\left(v_2 - v_1\right) + g_{mi}\left(v_{i1} - v_1\right) + g_{oi}\left(v_{out} - v_1\right) + g_{mi}\left(v_{i2} - v_1\right) &= 0 \\ g_{ol}v_{out} + g_{ml}v_2 + g_{oi}\left(v_{out} - v_1\right) + g_{mi}\left(v_{i2} - v_1\right) &= 0 \end{split}$$



#### • Tensión de salida $v_{out}$ :

$$(g_{mi} + g_{oi})v_1 - (g_{ml} + g_{oi})v_2 = g_{mi}v_{i1}$$

$$(2g_{mi} + 2g_{oi} + g_{o})v_1 - g_{oi}v_2 - g_{oi}v_{out} = g_{mi}v_{i1} + g_{mi}v_{i2}$$

$$(g_{mi} + g_{oi})v_1 - g_{ml}v_2 - (g_{oi} + g_{ol})v_{out} = g_{mi}v_{i2}$$

$$v_{out} = \frac{g_{mi}g_{ml}\left(2(g_{mi} + g_{oi})(v_{i1} - v_{i2}) + g_o\left(v_{i1} - \left(1 + \frac{g_{oi}}{g_{ml}}\right)v_{i2}\right)\right)}{(g_{mi} + g_{oi})(g_{oi}g_{ol} + 2g_{ml}(g_{oi} + g_{ol})) + g_o(g_{ml} + g_{oi})(g_{oi} + g_{ol})}$$

$$v_{out} = \frac{g_{mi}g_{ml}\left(2(g_{mi} + g_{oi}) + g_o\left(1 + \frac{g_{oi}}{2g_{ml}}\right)\right)(v_{i1} - v_{i2}) - g_{mi}g_{oi}g_o\frac{(v_{i1} + v_{i2})}{2}}{(g_{mi} + g_{oi})(g_{oi}g_{ol} + 2g_{ml}(g_{oi} + g_{ol})) + g_o(g_{ml} + g_{oi})(g_{oi} + g_{ol})}$$



• Ganancias DM  $(A_{dm})$  y CM  $(A_{cm})$ :

$$v_{out} = A_{dm} (v_{i1} - v_{i2}) + A_{cm} \frac{(v_{i1} + v_{i2})}{2}$$

$$A_{dm} = \frac{g_{mi}g_{ml}\left(2(g_{mi} + g_{oi}) + g_{o}\left(1 + \frac{g_{oi}}{2g_{ml}}\right)\right)}{(g_{mi} + g_{oi})(g_{oi}g_{ol} + 2g_{ml}(g_{oi} + g_{ol})) + g_{o}(g_{ml} + g_{oi})(g_{oi} + g_{ol})}$$

$$A_{cm} = \frac{-g_{mi}g_{oi}g_{o}}{(g_{mi} + g_{oi})(g_{oi}g_{ol} + 2g_{ml}(g_{oi} + g_{ol})) + g_{o}(g_{ml} + g_{oi})(g_{oi} + g_{ol})}$$

Razón de rechazo del modo común (CMMR):

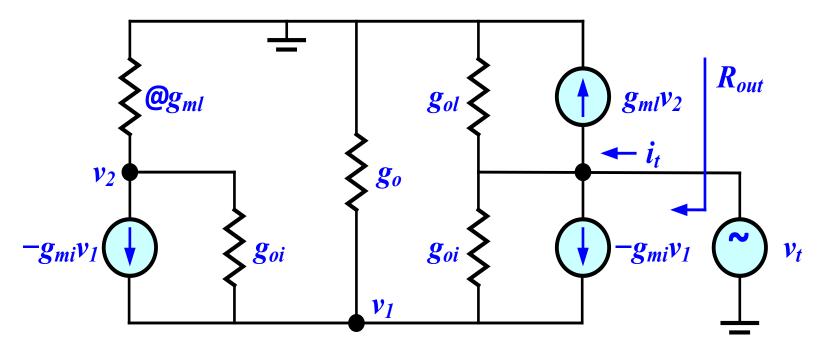
$$CMRR = \left| \frac{A_{dm}}{A_{cm}} \right| = \frac{g_{ml}}{g_{oi}g_o} (2(g_{mi} + g_{oi}) + g_o) + \frac{1}{2}$$

• Expresiones simplificadas:  $g_{mi}, g_{ml} >> g_o, g_{oi}, g_{ol}$ 

$$A_{dm}$$
;  $\frac{g_{mi}}{g_{oi} + g_{ol}}$   $A_{cm}$ ;  $\frac{-g_{o}g_{oi}}{2g_{ml}(g_{oi} + g_{ol})}$ 

$$CMRR; \frac{2g_{mi}g_{ml}}{g_{o}g_{oi}}$$

• Resistencia de salida  $R_{out}$ :



$$g_{ml}v_2 - g_{mi}v_1 + g_{oi}(v_2 - v_1) = 0$$

$$-g_ov_1 + g_{oi}(v_2 - v_1) - g_{mi}v_1 + g_{oi}(v_t - v_1) - g_{mi}v_1 = 0$$

$$g_{ol}v_t + g_{ml}v_2 + g_{oi}(v_t - v_1) - g_{mi}v_1 = i_t$$

#### Cálculo de R<sub>out</sub>:

$$(g_{mi} + g_{oi})v_1 - (g_{ml} + g_{oi})v_2 = 0$$

$$(2g_{mi} + 2g_{oi} + g_o)v_1 - g_{oi}v_2 - g_{oi}v_t = 0$$

$$(g_{mi} + g_{oi})v_1 - g_{ml}v_2 - (g_{oi} + g_{ol})v_t = -i_t$$

$$R_{out} = \frac{v_t}{i_t}$$

$$R_{out} = \frac{\left(g_{mi} + g_{oi}\right)\!\left(2g_{ml} + g_{oi}\right) + g_{o}\left(g_{ml} + g_{oi}\right)}{\left(g_{mi} + g_{oi}\right)\!\left(g_{oi}g_{ol} + 2g_{ml}\left(g_{oi} + g_{ol}\right)\right) + g_{o}\left(g_{ml} + g_{oi}\right)\!\left(g_{oi} + g_{ol}\right)}$$

$$g_{mi}, g_{ml} >> g_o, g_{oi}, g_{oi}: R_{out}; \frac{1}{g_{oi} + g_{ol}}$$